

# The physics of small systems: what to expect in eA given the “ridge” in pA and high multiplicity pp

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In collaboration with Jordan Singer and Kevin Welsh

EIC UG Mtg. 2016, 1/7/16

# Overview

- 1 The big picture
- 2 Flow in small systems?
  - Flow in small systems?
  - Do small systems behave hydrodynamically?
  - Collectivity in small systems
  - Initial-state momentum correlations?
- 3 What is needed to resolve this ambiguity?
  - What is needed?
  - What is missing?
- 4 Proton substructure: what does a proton look like in position space?
  - CGC picture of the nucleon
  - Modeling quark substructure of the nucleon
  - Characteristics of initial entropy density distributions in pp and light-heavy collisions
- 5 How can the EIC help?

# The big picture

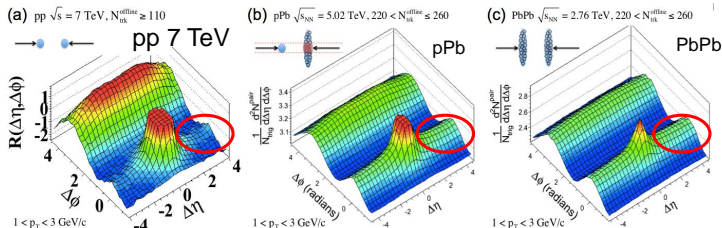
- Flow-like signatures of similar characteristics as those in AA collisions were also seen in pA and high-multiplicity pp.
- Seen in both single-particle observables (“radial flow”) and two-particle correlations (“anisotropic flow”).
- Initial-state momentum correlations can also manifest themselves as “anisotropic flow” in the final state, especially in small collision systems where they may survive final-state interactions.
- **What is the true origin of these flow-like signatures? How can we separate initial-state from final-state effects, in particular in small systems?**
- **What is the internal phase-space structure of a proton?**

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Flow in small systems?

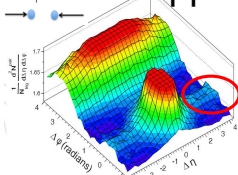
# Ridge in pp, pPb and PbPb



NEW

CMS pp  $\sqrt{s} = 13$  TeV,  $N_{\text{ch}}^{\text{offline}} \geq 105$   
1 <  $p_T$  < 3 GeV/c

## pp 13 TeV



Zhenyu Chen

CMS-FSQ-15-002

Ridge observed in high multiplicity  
pp collisions at **13 TeV** !



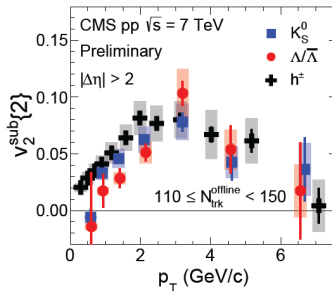
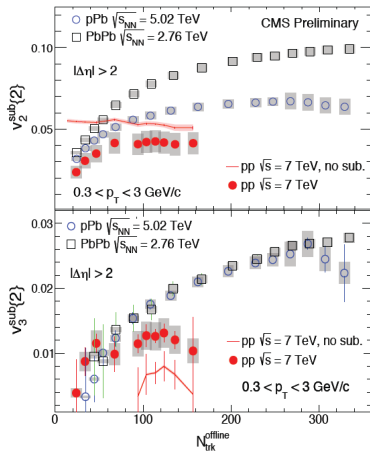
## 13 TeV vs. 7 TeV?

# Long-range correlations in high-mult. pp

Z. Chen

CMS-HIN-15-009

## Flow parameter analysis



- $v_2(\text{pp}) < v_2(\text{pPb}) < v_2(\text{PbPb})$
- $v_3(\text{pp}) \approx v_3(\text{pPb}) \approx v_3(\text{PbPb})$ , but  $v_3(\text{pp})$  deviates for  $N_{\text{trk}}^{\text{offline}} \gtrsim 90$
- Mass ordering for  $v_2^{\text{sub}\{2\}}$  at low  $p_T$



Byungsik Hong

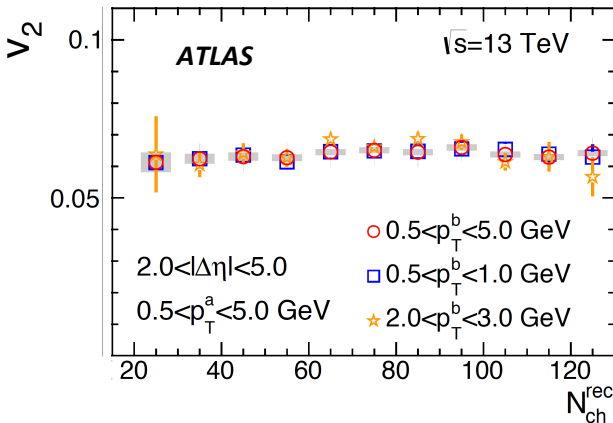
Quark Matter 2015, Kobe

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Flow in small systems?

# Flow in small systems?

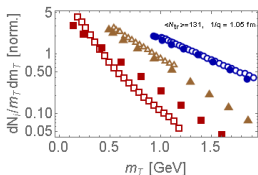


No centrality dependence of elliptic flow in pp?!

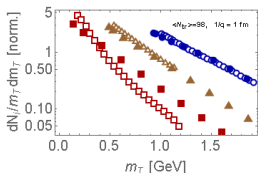
Flow not just in high-multiplicity pp?!

Not flow but something else?

# Flow in small systems?

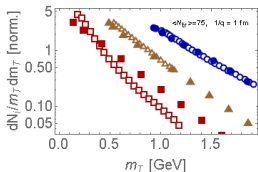


Kalaydzhyan & Shuryak PRC91 (2015) 054913



Open symbols: CMS data;  
filled symbols: Glubser flow

*K-p* mass splitting of  $m_T$ -slopes increases  
with *pp* multiplicity

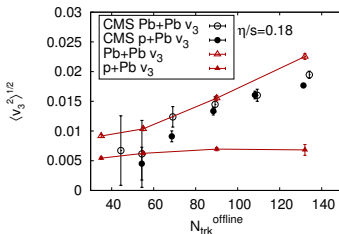
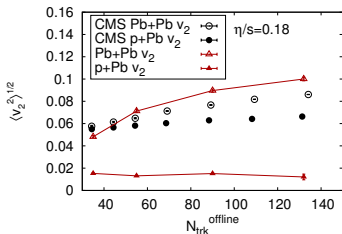
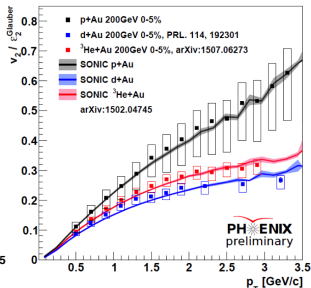
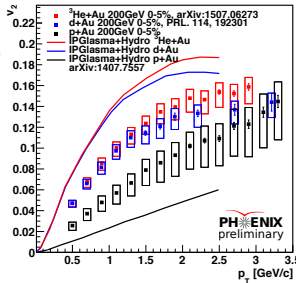
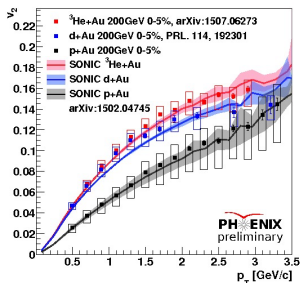


Radial flow in *pp*?

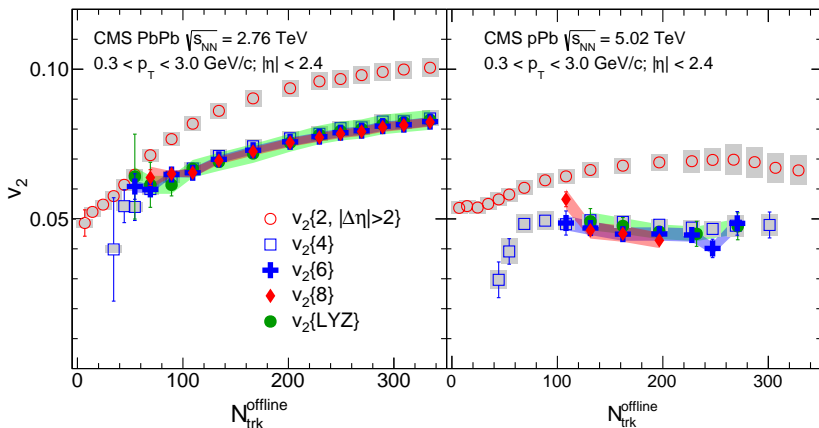


Do small systems behave hydrodynamically?

## Do small systems behave hydrodynamically?



# Collectivity in small systems!

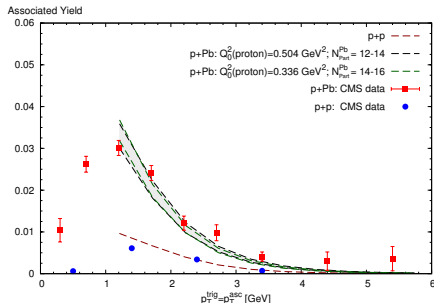
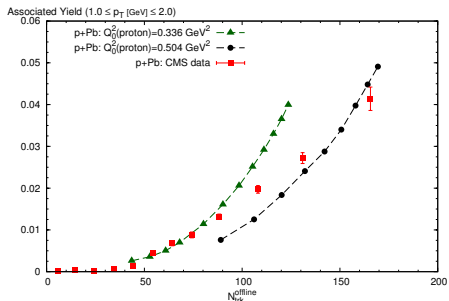


Whatever its origin, the “flow signal” represents a collective response (to what?) of all particles!

Initial-state momentum correlations?

# Initial-state momentum correlations?

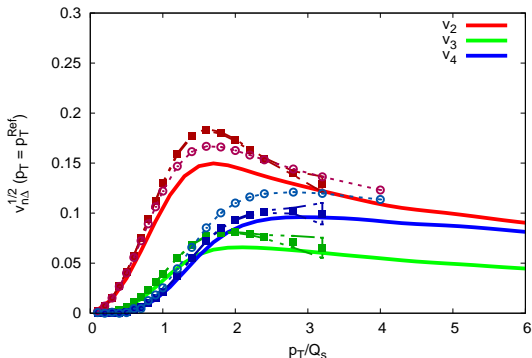
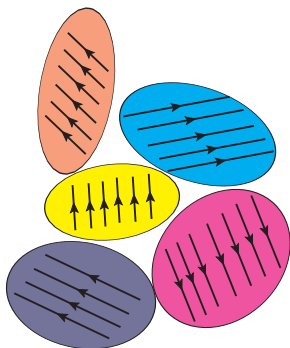
Dusling and Venugopalan, PRD87 (2013) 054014



Initial-state momentum (anti-)correlations from “Glasma graphs” qualitatively explain the multiplicity dependence and  $p_T$ -dependence at high  $p_T$  of the **ridge yields** in pPb and high-multiplicity pp collisions

# Initial-state momentum correlations?

Lappi, Schenke, Schlichting, Venugopalan, JHEP 2016 (arXiv:1509.03499)



Spatial inhomogeneity of CGC and spatial deformation of CGC regions of homogeneity generate momentum anisotropies among the initially produced partons, corresponding to non-zero  $v_n$  for all  $n$ , with “reasonable-looking”  $p_T$  dependence.

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# What is needed to resolve this ambiguity?

- Initial conditions for the phase-space distribution of the produced matter,

$$f_{\text{matter}}(x_{\perp}, \phi_s; p_{\perp}, \phi_p; y_p - \eta_s; \tau_0)$$

which depends on the

- phase-space (Wigner) distribution of the glue inside the nucleons bound into small nuclei:

$$f_{\text{glue}}(x_{\perp}, \phi_s; k_{\perp}, \phi_k; y_k - \eta_s; \tau_0)$$

- From  $f_{\text{matter}}$  we obtain the initial energy-momentum tensor

$$T^{\mu\nu}(x_{\perp}, \eta_s, \tau_0) = \frac{\nu_{\text{dof}}}{(2\pi)^3} \int dy_p d^2 p_{\perp} p^{\mu} p^{\nu} f_{\text{matter}}(x_{\perp}, \phi_s; p_{\perp}, \phi_p; y_p - \eta_s; \tau_0)$$

# What is needed to resolve this ambiguity?

- Once the initial  $T^{\mu\nu}(x)$  is known, we can evolve it for some time  $\tau_{\text{eq}} - \tau_0$  with a pre-equilibrium model, match it to viscous hydrodynamic form,

$$T^{\mu\nu} = eu^\mu u^\nu - (P(e) + \Pi)\Delta^{\mu\nu} + \pi^{\mu\nu},$$

run it through viscous hydrodynamics plus hadronic afterburner, and compare its output with experiment.

- To account for event-by-event quantum fluctuations in the initial  $T^{\mu\nu}(x)$ , and for thermal noise during the evolution, the dynamical evolution must be performed many times before taking ensemble averages as done in experiment.

What is missing?

# What is missing in present calculations?

## Present modeling uses simplified assumptions for the initial phase-space distrib'n:

- Few models account for the initial momentum structure of the medium; most ignore it completely.  $\Rightarrow$  **incorrect/unreliable initial conditions for  $\Pi, \pi^{\mu\nu}$**
- While granularity of the initial spatial density distribution **is accounted for at the nucleon length scale**, by Monte-Carlo sampling the nucleon positions from a smooth Woods-Saxon probability distribution before allowing them to collide and lose energy to create lower-rapidity secondary matter, **quantum fluctuations on sub-nucleonic length scales are poorly controlled and mostly ignored. IP-Glasma includes sub-nucleonic gluon field fluctuations, but appears to get them wrong**, yielding spatial gluon distributions inside protons that are too compact.
- Most approaches (e.g. PHOBOS Glauber Monte Carlo) use disk-like nucleons for computing the collision probability. More realistic collision detection using Gaussian nucleons is implemented in GLISSANDO and iEBE-VISHNU.
- Most approaches ignore quantum fluctuations in the amount of beam energy lost to lower rapidities in a NN collision. Without these, the measured KNO-like multiplicity distributions in pp collisions are not reproduced, and pp collisions produce zero  $\epsilon_3$  by symmetry. GLISSANDO and iEBE-VISHNU include pp multiplicity fluctuations, creating non-zero triangularity in pp, even without sub-nucleonic structure.



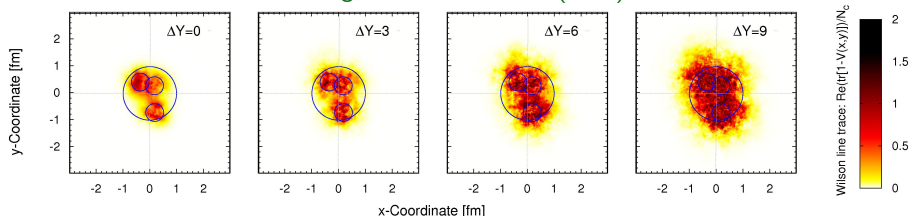
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CGC picture of the nucleon

# “Three quarks for Muster Mark!”

Schlichting, Schenke, PLB739 (2014) 313



- 3 valence quarks act as large- $x$  color sources of the low- $x$  gluon fields.
- Spatial positions of quarks at the instant of collision fluctuate from event to event and generate a lumpy color distribution at large  $x$ .
- This lumpiness is tracked by the quarks' gluon clouds, becoming more diffuse at smaller  $x \Rightarrow$  triune lumpiness of the gluon fields inside the nucleon when viewed through midrapidity particle production, with an intrinsic length scale (“gluonic radius of a quark”) that appears to grow with collision energy.
- $\Rightarrow$  Protons have just as much intrinsic triangularity as  $^3\text{He}$  nuclei, just on a shorter length scale. But in p+A **all** particle production occurs on a smaller length scale than in  $^3\text{He}+A$ ! This affects mostly radial flow, though.

# Modeling quark substructure of the nucleon I

(Ongoing work with undergraduates [Jordan Singer](#) and [Kevin Welsh](#))

- The gluon field density inside the proton is the **sum of three 3-d Gaussians** of norm  $\frac{1}{3}$  and width  $\sigma_g$  (representing the gluon clouds around the valence quarks). **Default value:**  $\sigma_g = 0.3 \text{ fm}$  (best fit of pPb mult. dist. at LHC)
- The quark positions (centers of the gluon clouds) are sampled from a 3-d Gaussian with width  $\sigma_q$  around the center of the nucleon, requiring their center of mass to coincide with the nucleon center.
- The widths are constrained by  $\sigma_g^2 + \frac{2}{3}\sigma_q^2 = B$  such that the average proton density is a normalized Gaussian

$$\langle \rho_p(\mathbf{r}) \rangle = \frac{e^{-\frac{r^2}{2B}}}{(2\pi B)^{2/3}}$$

with  $\sqrt{s}$ -dependent width  $B(\sqrt{s}) = \frac{\sigma_{NN}^{\text{inel}}(\sqrt{s})}{8\pi}$ , to reproduce the measured inelastic NN cross section.

# Modeling quark substructure of the nucleon II

- Projecting  $\rho_p$  along  $z$  gives the nucleon thickness function  $T_N(\mathbf{r}_\perp)$  in the transverse plane.
- Folding two nucleon thickness functions yields the nucleon-nucleon overlap function  $T_{NN}(\mathbf{b})$  at impact parameter  $\mathbf{b}$  (which actually depends on all 6 quark positions), from which the probability for each of the two nucleons to get wounded in the collision is computed as

$$P_{ij}(\mathbf{r}_{\perp i} - \mathbf{r}_{\perp j}) = 1 - \exp[-\sigma_{gg} T_{NN}(\mathbf{r}_{\perp i} - \mathbf{r}_{\perp j})]$$

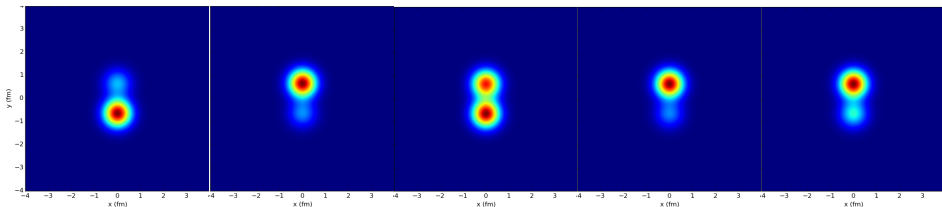
where  $i$  and  $j$  are from projectile and target, respectively. The gluon-gluon cross section  $\sigma_{gg}$  is determined by the normalization of  $P_{ij}$  to the inelastic NN cross section.

- For each wounded nucleon, all three quarks are assumed to contribute to energy production at midrapidity, with a Gaussian density profile of width  $\sigma_g$  and **independently fluctuating ( $\Gamma$ -distributed) normalization**, with variance adjusted to reproduce measured pp multiplicity distributions.

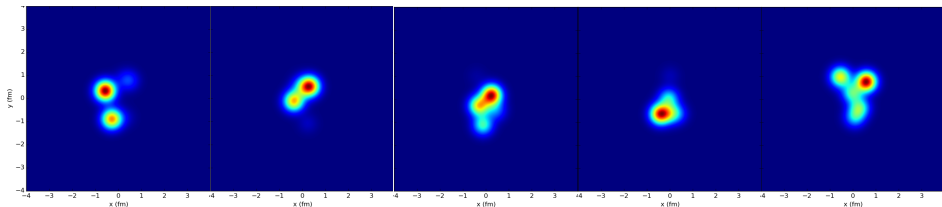
Characteristics of initial entropy density distributions in pp and light-heavy collisions

# Initial entropy density in $b=1.3$ fm pp collisions

smooth Gaussian protons:



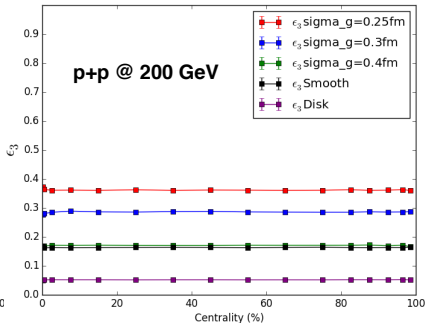
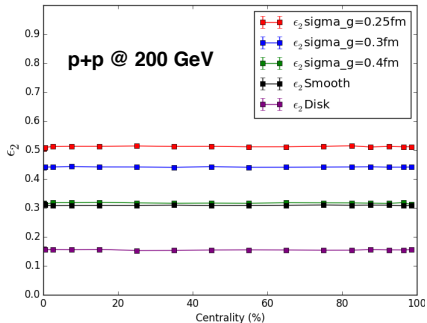
protons with fluctuating quark substructure ( $\sigma_g = 0.3$  fm):



For protons with quark substructure the Gaussian collision criterium appears to favor somewhat more compact distributions of produced entropy density

Characteristics of initial entropy density distributions in pp and light-heavy collisions

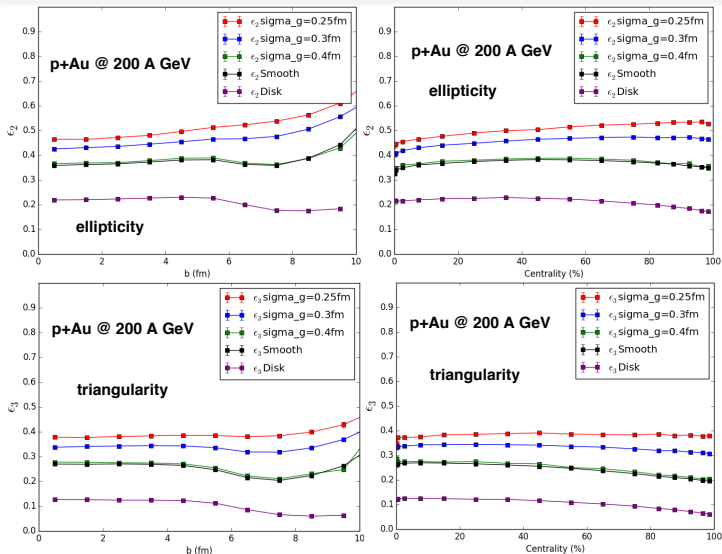
$\varepsilon_{2,3}$  vs. centrality: pp @  $\sqrt{s}=200$  A GeV



- Ellipticity and triangularity show strong sensitivity to  $\sigma_g$ .
- Since  $\sqrt{B} = 0.408$  fm at  $\sqrt{s} = 200$  GeV, quark subdivision with  $\sigma_g = 0.4$  fm is almost indistinguishable from a smooth Gaussian proton.
- Disk-like collision detection gives smallest eccentricities.

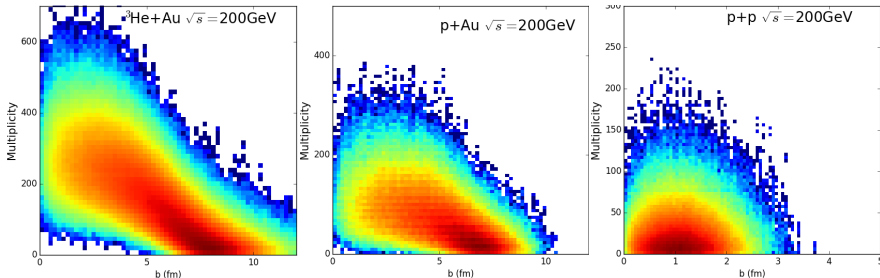
Characteristics of initial entropy density distributions in pp and light-heavy collisions

$\epsilon_{2,3}$  vs. centrality: p+Au @  $\sqrt{s}=200$  A GeV



Characteristics of initial entropy density distributions in pp and light-heavy collisions

In p+p and light+heavy “centrality” does not measure b!



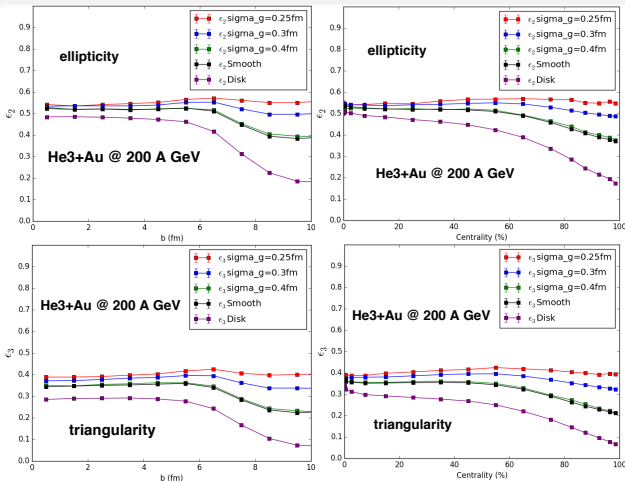
pp multiplicity fluctuations destroy strong anticorrelation between multiplicity and impact parameter seen in Au+Au and Pb+Pb

⇒ “centrality” measured by multiplicity is a misnomer in collisions involving light projectiles



Characteristics of initial entropy density distributions in pp and light-heavy collisions

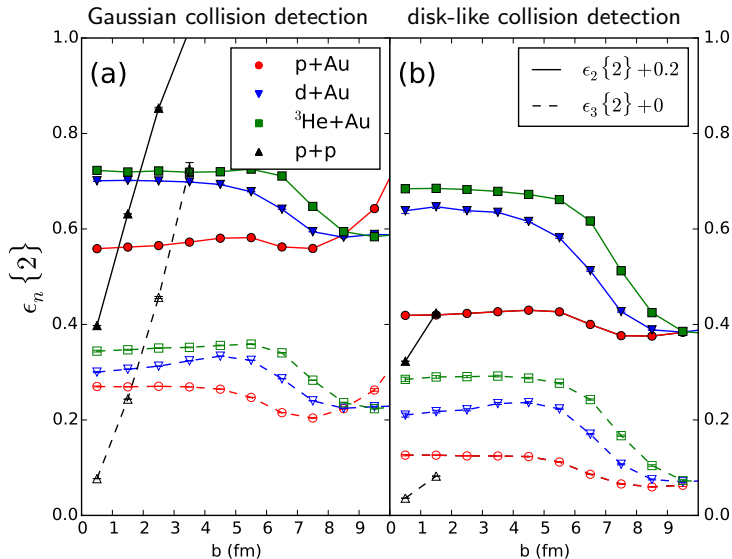
$\varepsilon_{2,3}$  vs. centrality:  $^3\text{He}+\text{Au}$  @  $\sqrt{s}=200$  A GeV



Reduced sensitivity to p-substructure and  $\sigma_g$  for larger projectiles, except in peripheral events

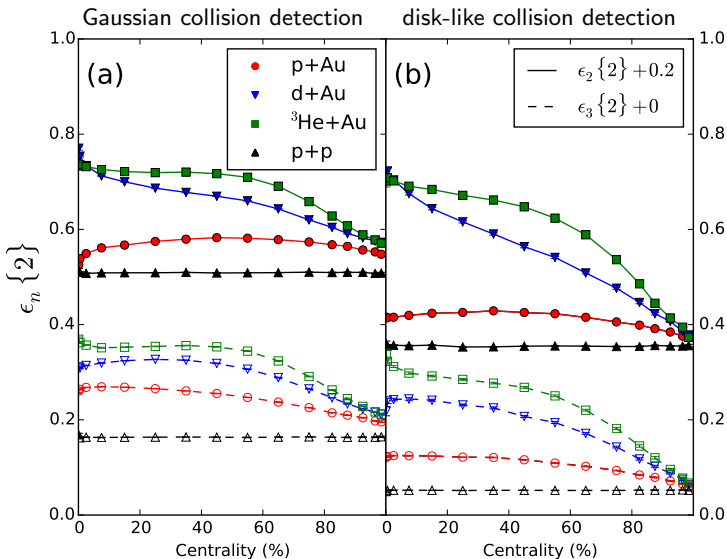
Characteristics of initial entropy density distributions in pp and light-heavy collisions

# $\epsilon_{2,3}$ vs. impact parameter for different collision systems



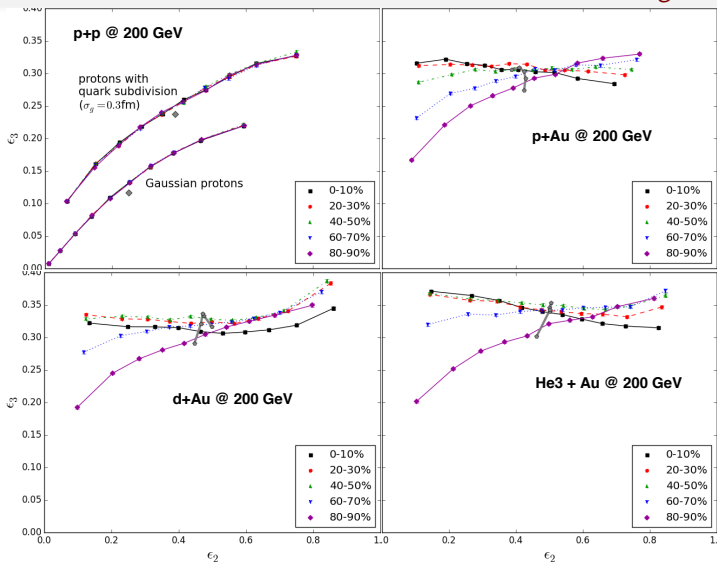
Characteristics of initial entropy density distributions in pp and light-heavy collisions

# $\epsilon_{2,3}$ vs. “centrality” for different collision systems



Characteristics of initial entropy density distributions in pp and light-heavy collisions

# $\epsilon_2$ - $\epsilon_3$ correlations: pp & light-heavy collisions, $\sigma_g = 0.3$ fm



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# How can the EIC help?

- Measure the average gluon Wigner distribution

$$\langle f_{\text{glue}}(x_{\perp}, \phi_s; k_{\perp}, \phi_k; y_k - \eta_s) \rangle$$

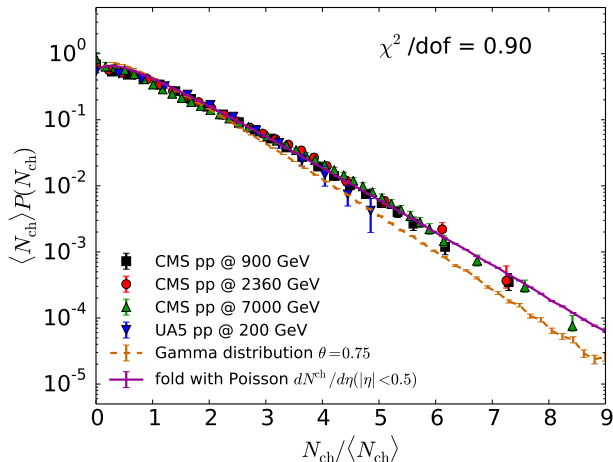
and its fluctuation spectrum in  $e+A$  for  $A=p, d, {}^3\text{He}, \dots$

- As we learned from the study of flow coefficients  $v_n$  in heavy-ion collisions, this requires to measure different types of two-particle correlations that access different moments of the probability distributions for  $f_{\text{glue}}$  and/or its (spatial) azimuthal Fourier moments.
- I don't know how to do this, but I am sure the theory for such measurements can be developed along the same lines as for the GPDs which are the zeroth Fourier moment of  $f_{\text{glue}}$ .

# The End

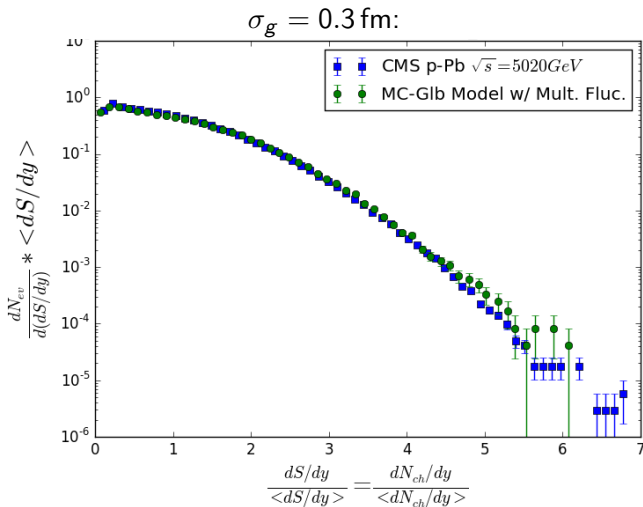
# pp multiplicity distribution

Same for smooth Gaussian and quark-subdivided protons, after rescaling of the  $\Gamma$ -distribution:





# pPb multiplicity distribution



# $\epsilon_{2,3}$ vs. centrality: d+Au @ $\sqrt{s}=200$ A GeV

